









From Digital Design by Mano, 2nd edition, 1991.

**TABLE 2-7**  
Truth Tables for the 16 Functions of Two Binary Variables

| x               | y | F <sub>0</sub> | F <sub>1</sub> | F <sub>2</sub> | F <sub>3</sub> | F <sub>4</sub> | F <sub>5</sub> | F <sub>6</sub> | F <sub>7</sub> | F <sub>8</sub> | F <sub>9</sub> | F <sub>10</sub> | F <sub>11</sub> | F <sub>12</sub> | F <sub>13</sub> | F <sub>14</sub> | F <sub>15</sub> |
|-----------------|---|----------------|----------------|----------------|----------------|----------------|----------------|----------------|----------------|----------------|----------------|-----------------|-----------------|-----------------|-----------------|-----------------|-----------------|
| 0               | 0 | 0              | 0              | 0              | 0              | 0              | 0              | 0              | 0              | 1              | 1              | 1               | 1               | 1               | 1               | 1               | 1               |
| 0               | 1 | 0              | 0              | 0              | 0              | 1              | 1              | 1              | 1              | 0              | 0              | 0               | 0               | 1               | 1               | 1               | 1               |
| 1               | 0 | 0              | 0              | 1              | 1              | 0              | 0              | 1              | 1              | 0              | 0              | 1               | 1               | 0               | 0               | 1               | 1               |
| 1               | 1 | 0              | 1              | 0              | 1              | 0              | 1              | 0              | 1              | 0              | 1              | 0               | 1               | 0               | 1               | 0               | 1               |
| Operator symbol |   | .              | /              | /              | /              | /              | ⊕              | +              | ↓              | ⊙              | ⊕              | +               | ↓               | ⊙               | ⊃               | '               | ⊃               |

**TABLE 2-8**  
Boolean Expressions for the 16 Functions of Two Variables

| Boolean functions          | Operator symbol | Name         | Comments            |
|----------------------------|-----------------|--------------|---------------------|
| F <sub>0</sub> = 0         |                 | Null         | Binary constant 0   |
| F <sub>1</sub> = xy        | x · y           | AND          | x and y             |
| F <sub>2</sub> = xy'       | x/y             | Inhibition   | x but not y         |
| F <sub>3</sub> = x         |                 | Transfer     | x                   |
| F <sub>4</sub> = x'y       | y/x             | Inhibition   | y but not x         |
| F <sub>5</sub> = y         |                 | Transfer     | y                   |
| F <sub>6</sub> = xy' + x'y | x ⊕ y           | Exclusive-OR | x or y but not both |
| F <sub>7</sub> = x + y     | x + y           | OR           | x or y              |
| F <sub>8</sub> = (x + y)'  | x ↓ y           | NOR          | Not-OR              |
| F <sub>9</sub> = xy + x'y' | x ⊙ y           | Equivalence  | x equals y          |
| F <sub>10</sub> = y'       | y'              | Complement   | Not y               |
| F <sub>11</sub> = x + y'   | x ⊃ y           | Implication  | If y then x         |
| F <sub>12</sub> = x'       | x'              | Complement   | Not x               |
| F <sub>13</sub> = x' + y   | x ⊃ y           | Implication  | If x then y         |
| F <sub>14</sub> = (xy)'    | x ↑ y           | NAND         | Not-AND             |
| F <sub>15</sub> = 1        |                 | Identity     | Binary constant 1   |

| Name                         | Graphic symbol  | Algebraic function           | Truth table   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |
|------------------------------|---|------------------------------|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|
| AND                          |    | $F = xy$                     | <table border="1"> <tr><th>x</th><th>y</th><th>F</th></tr> <tr><td>0</td><td>0</td><td>0</td></tr> <tr><td>0</td><td>1</td><td>0</td></tr> <tr><td>1</td><td>0</td><td>0</td></tr> <tr><td>1</td><td>1</td><td>1</td></tr> </table> | x | y | F | 0 | 0 | 0 | 0 | 1 | 0 | 1 | 0 | 0 | 1 | 1 | 1 |
| x                            | y   | F                            |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |
| 0                            | 0   | 0                            |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |
| 0                            | 1   | 0                            |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |
| 1                            | 0   | 0                            |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |
| 1                            | 1   | 1                            |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |
| OR                           |    | $F = x + y$                  | <table border="1"> <tr><th>x</th><th>y</th><th>F</th></tr> <tr><td>0</td><td>0</td><td>0</td></tr> <tr><td>0</td><td>1</td><td>1</td></tr> <tr><td>1</td><td>0</td><td>1</td></tr> <tr><td>1</td><td>1</td><td>1</td></tr> </table> | x | y | F | 0 | 0 | 0 | 0 | 1 | 1 | 1 | 0 | 1 | 1 | 1 | 1 |
| x                            | y   | F                            |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |
| 0                            | 0   | 0                            |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |
| 0                            | 1   | 1                            |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |
| 1                            | 0   | 1                            |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |
| 1                            | 1   | 1                            |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |
| Inverter                     |    | $F = x'$                     | <table border="1"> <tr><th>x</th><th>F</th></tr> <tr><td>0</td><td>1</td></tr> <tr><td>1</td><td>0</td></tr> </table>   | x | F | 0 | 1 | 1 | 0 |   |   |   |   |   |   |   |   |   |
| x                            | F   |                              |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |
| 0                            | 1   |                              |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |
| 1                            | 0   |                              |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |
| Buffer                       |    | $F = x$                      | <table border="1"> <tr><th>x</th><th>F</th></tr> <tr><td>0</td><td>0</td></tr> <tr><td>1</td><td>1</td></tr> </table>   | x | F | 0 | 0 | 1 | 1 |   |   |   |   |   |   |   |   |   |
| x                            | F   |                              |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |
| 0                            | 0   |                              |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |
| 1                            | 1   |                              |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |
| NAND                         |    | $F = (xy)'$                  | <table border="1"> <tr><th>x</th><th>y</th><th>F</th></tr> <tr><td>0</td><td>0</td><td>1</td></tr> <tr><td>0</td><td>1</td><td>1</td></tr> <tr><td>1</td><td>0</td><td>1</td></tr> <tr><td>1</td><td>1</td><td>0</td></tr> </table> | x | y | F | 0 | 0 | 1 | 0 | 1 | 1 | 1 | 0 | 1 | 1 | 1 | 0 |
| x                            | y   | F                            |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |
| 0                            | 0   | 1                            |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |
| 0                            | 1   | 1                            |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |
| 1                            | 0   | 1                            |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |
| 1                            | 1   | 0                            |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |
| NOR                          |  | $F = (x + y)'$               | <table border="1"> <tr><th>x</th><th>y</th><th>F</th></tr> <tr><td>0</td><td>0</td><td>1</td></tr> <tr><td>0</td><td>1</td><td>0</td></tr> <tr><td>1</td><td>0</td><td>0</td></tr> <tr><td>1</td><td>1</td><td>0</td></tr> </table> | x | y | F | 0 | 0 | 1 | 0 | 1 | 0 | 1 | 0 | 0 | 1 | 1 | 0 |
| x                            | y   | F                            |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |
| 0                            | 0   | 1                            |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |
| 0                            | 1   | 0                            |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |
| 1                            | 0   | 0                            |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |
| 1                            | 1   | 0                            |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |
| Exclusive-OR (XOR)           |  | $F = xy' + x'y = x \oplus y$ | <table border="1"> <tr><th>x</th><th>y</th><th>F</th></tr> <tr><td>0</td><td>0</td><td>0</td></tr> <tr><td>0</td><td>1</td><td>1</td></tr> <tr><td>1</td><td>0</td><td>1</td></tr> <tr><td>1</td><td>1</td><td>0</td></tr> </table> | x | y | F | 0 | 0 | 0 | 0 | 1 | 1 | 1 | 0 | 1 | 1 | 1 | 0 |
| x                            | y   | F                            |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |
| 0                            | 0   | 0                            |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |
| 0                            | 1   | 1                            |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |
| 1                            | 0   | 1                            |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |
| 1                            | 1   | 0                            |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |
| Exclusive-NOR or equivalence |  | $F = xy + x'y' = x \odot y$  | <table border="1"> <tr><th>x</th><th>y</th><th>F</th></tr> <tr><td>0</td><td>0</td><td>1</td></tr> <tr><td>0</td><td>1</td><td>0</td></tr> <tr><td>1</td><td>0</td><td>0</td></tr> <tr><td>1</td><td>1</td><td>1</td></tr> </table> | x | y | F | 0 | 0 | 1 | 0 | 1 | 0 | 1 | 0 | 0 | 1 | 1 | 1 |
| x                            | y   | F                            |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |
| 0                            | 0   | 1                            |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |
| 0                            | 1   | 0                            |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |
| 1                            | 0   | 0                            |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |
| 1                            | 1   | 1                            |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |

**FIGURE 2-5**  
Digital logic gates