## A postfix "language" for lab 3

We can combine the rules for a postfix expression with a rule for declaring or initializing a variable to create a simple calculator language. This language is similar to the one in the textbook, but a little simpler because of the use of postfix rather than infix expressions.

```
prog }->\mathrm{ stmt | stmt prog
stmt }->\mathrm{ id = num ; | expr ;
expr }->\mathrm{ id | num | expr expr op
op}->+|-|*|
```

It turns out that the bottom-up parse table is as follows. In the reduce entries, I've abbreviated the names of the nonterminals to just their first letter.

| State | id | $=$ | num | $;$ | + | - | $*$ | $/$ | $\$$ | prog | stmt | expr | op |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| 0 | 2 |  | 4 |  |  |  |  |  |  |  | 1 | 3 |  |
| 1 | 2 |  | 4 |  |  |  |  |  | $\odot$ | 5 | 1 | 3 |  |
| 2 | $-1, \mathrm{E}$ | 6 | $-1, \mathrm{E}$ | $-1, \mathrm{E}$ | $-1, \mathrm{E}$ | $-1, \mathrm{E}$ | $-1, \mathrm{E}$ | $-1, \mathrm{E}$ |  |  |  |  |  |
| 3 | 2 |  | 4 | 7 |  |  |  |  |  |  |  | 8 |  |
| 4 | $-1, \mathrm{E}$ |  | $-1, \mathrm{E}$ | $-1, \mathrm{E}$ | $-1, \mathrm{E}$ | $-1, \mathrm{E}$ | $-1, \mathrm{E}$ | $-1, \mathrm{E}$ |  |  |  |  |  |
| 5 |  |  |  |  |  |  |  |  | $\odot$ |  |  |  |  |
| 6 |  |  | 9 |  |  |  |  |  |  |  |  |  |  |
| 7 | $-2, \mathrm{~S}$ |  | $-2, \mathrm{~S}$ |  |  |  |  |  | $-2, \mathrm{~S}$ |  |  |  |  |
| 8 | 2 |  | 4 |  | 11 | 12 | 13 | 14 |  |  |  | 8 | 10 |
| 9 |  |  |  | 15 |  |  |  |  |  |  |  |  |  |
| 10 | $-3, \mathrm{E}$ |  | $-3, \mathrm{E}$ | $-3, \mathrm{E}$ | $-3, \mathrm{E}$ | $-3, \mathrm{E}$ | $-3, \mathrm{E}$ | $-3, \mathrm{E}$ |  |  |  |  |  |
| 11 | $-1, \mathrm{O}$ |  | $-1, \mathrm{O}$ | $-1, \mathrm{O}$ | $-1, \mathrm{O}$ | $-1, \mathrm{O}$ | $-1, \mathrm{O}$ | $-1, \mathrm{O}$ |  |  |  |  |  |
| 12 | $-1, \mathrm{O}$ |  | $-1, \mathrm{O}$ | $-1, \mathrm{O}$ | $-1, \mathrm{O}$ | $-1, \mathrm{O}$ | $-1, \mathrm{O}$ | $-1, \mathrm{O}$ |  |  |  |  |  |
| 13 | $-1, \mathrm{O}$ |  | $-1, \mathrm{O}$ | $-1, \mathrm{O}$ | $-1, \mathrm{O}$ | $-1, \mathrm{O}$ | $-1, \mathrm{O}$ | $-1, \mathrm{O}$ |  |  |  |  |  |
| 14 | $-1, \mathrm{O}$ |  | $-1, \mathrm{O}$ | $-1, \mathrm{O}$ | $-1, \mathrm{O}$ | $-1, \mathrm{O}$ | $-1, \mathrm{O}$ | $-1, \mathrm{O}$ |  |  |  |  |  |
| 15 | $-4, \mathrm{~S}$ |  | $-4, \mathrm{~S}$ |  |  |  |  |  | $-4, \mathrm{~S}$ |  |  |  |  |

As you can see, states $2,4,7,10-15$ contain reduce actions. Plus, states 1 and 5 are accept states, so these are reductions as well for the end of input. What semantic actions will we need to help us create a syntax tree? We probably won't be sure until we actually trace through some input to see what we'd expect.

Let's parse the input: a = 7 ; $9 \mathbf{a}$ *

| State stack | Input | Action | Semantic action we expect |
| :--- | :--- | :--- | :--- |
|  |  |  |  |
|  |  |  |  |
|  |  |  |  |


|  |  |  |  |
| :--- | :--- | :--- | :--- |
|  |  |  |  |
|  |  |  |  |
|  |  |  |  |
|  |  |  |  |
|  |  |  |  |
|  |  |  |  |
|  |  |  |  |
|  |  |  |  |
|  |  |  |  |
|  |  |  |  |
|  |  |  |  |
|  |  |  |  |
|  |  |  |  |
|  |  |  |  |
|  |  |  |  |
|  |  |  |  |
|  |  |  |  |
|  |  |  |  |
|  |  |  |  |
|  |  |  |  |
|  |  |  |  |
|  |  |  |  |
|  |  |  |  |
|  |  |  |  |
|  |  |  |  |
|  |  |  |  |
|  |  |  |  |
|  |  |  |  |
|  |  |  |  |
|  |  |  |  |
|  |  |  |  |
|  |  |  |  |

Let's write out semantic actions here. Can you tell how to figure out which production is being reduced? Do you think we may need some semantic actions for goto operations?

| state | Production being reduced | Create what? |
| :--- | :--- | :--- |
| 1 |  |  |
| 2 |  |  |
| 4 |  |  |
| 5 |  |  |
| 7 |  |  |
| 10 |  |  |
| 11 |  |  |
| 12 |  |  |
| 13 |  |  |
| 14 |  |  |
| 15 |  |  |

